

## ecl-es-halt<sup>11,40</sup>

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ecl-es-halt(es; x)
≡def ecl_ind(x;
  k, test.(λn, e1, e2. if (n =0 0)
  then e2 =
    first e ≥ e1.(es-kind(es; e) = k)
    c ∧ (↑(test(es-state-when(es; e), es-val(es; e))))
  else False
  fi );
  a, b, ha, hb.(λn, e1, e2. if (n =0 0) then False else ha(n, e1, e2) fi
  ∨ ∃e ∈ [e1, e2].(ha(0, e1, es-pred(es; e)) ∧ (hb(n, e, e2)));
  a, b, ha, hb.(λn, e1, e2. if (n =0 0)
  then ((ha(0, e1, e2)) ∧ ∃e ∈ [e1, e2].hb(0, e1, e))
    ∨ ((hb(0, e1, e2)) ∧ ∃e ∈ [e1, e2].ha(0, e1, e))
  else ((ha(n, e1, e2))
    ∧ l-all(cons(0; ecl-ex(b));
      m.if n ≤z m
      then ∀e ∈ [e1, e2].¬(hb(m, e1, e))
      else ∀e ∈ [e1, e2].¬(hb(m, e1, e))
      fi ))
    ∨ ((hb(n, e1, e2))
      ∧ l-all(cons(0; ecl-ex(a));
        m.if n ≤z m
        then ∀e ∈ [e1, e2].¬(ha(m, e1, e))
        else ∀e ∈ [e1, e2].¬(ha(m, e1, e))
        fi ))
    fi );
  a, b, ha, hb.(λn, e1, e2. ((ha(n, e1, e2))
  ∧ l-all(cons(0; ecl-ex(b));
    m.if n ≤z m
    then ∀e ∈ [e1, e2].¬(hb(m, e1, e))
    else ∀e ∈ [e1, e2].¬(hb(m, e1, e))
    fi ))
  ∨ ((hb(n, e1, e2))
    ∧ l-all(cons(0; ecl-ex(a));
      m.if n ≤z m
      then ∀e ∈ [e1, e2].¬(ha(m, e1, e))
      else ∀e ∈ [e1, e2].¬(ha(m, e1, e))
      fi )));
  a, ha.(λn, e1, e2. if (n =0 0)
  then False
  else [e1; e2]~([x, y].ha(0, x, y))*[x, y].ha(n, x, y)
  fi );

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$a, m, ha, ha;$   
 $a, m, ha.(\lambda n, e_1, e_2. \text{ if } (n =_0 0) \text{ then False else } ha(n, e_1, e_2) \text{ fi}$   
 $\vee \text{ if } (n =_0 m) \text{ then } ha(0, e_1, e_2) \text{ else False fi );}$   
 $a, l, ha.(\lambda n, e_1, e_2. ((ha(n, e_1, e_2)) \wedge (\neg(n \in l))))$   
 $\vee \text{ if } (n =_0 0) \text{ then } \text{Lexists}(l; \mathbb{N}; m. (ha(m, e_1, e_2))) \text{ else False fi )}$

*clarification:*

$\text{ecl-es-halt}(es; x)$   
 $\equiv_{\text{def}} \text{ecl\_ind}(x;$   
 $\quad k, test.(\lambda n, e_1, e_2. \text{ if } (n =_0 0)$   
 $\quad \text{then es-first-since}(es; e. (\text{es-kind}(es; e) = k \in \text{Knd}))$   
 $\quad \quad c \wedge (\uparrow(test(\text{es-state-when}(es; e), \text{es-val}(es; e))))); e_1; e_2)$   
 $\quad \text{else False}$   
 $\quad \text{fi );}$   
 $a, b, ha, hb.(\lambda n, e_1, e_2. \text{ if } (n =_0 0) \text{ then False else } ha(n, e_1, e_2) \text{ fi}$   
 $\vee \text{ existse-between3}(es; e_1; e_2; e. (ha(0, e_1, \text{es-pred}(es; e))) \wedge (hb(n, e, e_2)))));$   
 $a, b, ha, hb.(\lambda n, e_1, e_2. \text{ if } (n =_0 0)$   
 $\text{then } ((ha(0, e_1, e_2)) \wedge \text{existse-between2}(es; e_1; e_2; e. hb(0, e_1, e)))$   
 $\quad \vee ((hb(0, e_1, e_2)) \wedge \text{existse-between2}(es; e_1; e_2; e. ha(0, e_1, e)))$   
 $\text{else } ((ha(n, e_1, e_2))$   
 $\quad \wedge \text{l-all}(\text{cons}(0; \text{ecl-ex}(b));$   
 $\quad \quad m. \text{if } n \leq_z m$   
 $\quad \quad \text{then alle from } es \text{ in } [e_1; e_2]. \neg(hb(m, e_1, e))$   
 $\quad \quad \text{else alle-between2}(es; e_1; e_2; e. \neg(hb(m, e_1, e)))$   
 $\quad \quad \text{fi )}$   
 $\quad \vee ((hb(n, e_1, e_2))$   
 $\quad \quad \wedge \text{l-all}(\text{cons}(0; \text{ecl-ex}(a));$   
 $\quad \quad \quad m. \text{if } n \leq_z m$   
 $\quad \quad \quad \text{then alle from } es \text{ in } [e_1; e_2]. \neg(ha(m, e_1, e))$   
 $\quad \quad \quad \text{else alle-between2}(es; e_1; e_2; e. \neg(ha(m, e_1, e)))$   
 $\quad \quad \quad \text{fi )}$   
 $\quad \text{fi );}$   
 $a, b, ha, hb.(\lambda n, e_1, e_2. ((ha(n, e_1, e_2))$   
 $\wedge \text{l-all}(\text{cons}(0; \text{ecl-ex}(b));$   
 $\quad m. \text{if } n \leq_z m$   
 $\quad \text{then alle from } es \text{ in } [e_1; e_2]. \neg(hb(m, e_1, e))$   
 $\quad \text{else alle-between2}(es; e_1; e_2; e. \neg(hb(m, e_1, e)))$   
 $\quad \text{fi )}$   
 $\vee ((hb(n, e_1, e_2))$   
 $\quad \wedge \text{l-all}(\text{cons}(0; \text{ecl-ex}(a));$   
 $\quad \quad m. \text{if } n \leq_z m$   
 $\quad \quad \text{then alle from } es \text{ in } [e_1; e_2]. \neg(ha(m, e_1, e))$   
 $\quad \quad \text{else alle-between2}(es; e_1; e_2; e. \neg(ha(m, e_1, e)))$   
 $\quad \quad \text{fi }));$   
 $a, ha.(\lambda n, e_1, e_2. \text{ if } (n =_0 0)$

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then False
else es-pstar-q(es; x, y.ha(0, x, y); x, y.ha(n, x, y); e1; e2)
fi );
a, m, ha. ha;
a, m, ha.( $\lambda n, e_1, e_2.$  if (n =0 0) then False else ha(n, e1, e2) fi
 $\vee$  if (n =0 m) then ha(0, e1, e2) else False fi );
a, l, ha.( $\lambda n, e_1, e_2.$  ((ha(n, e1, e2))  $\wedge$  ( $\neg$ (n  $\in$  l  $\in$   $\mathbb{N}$ )))
 $\vee$  if (n =0 0) then  $\exists$ exists(l;  $\mathbb{N}$ ; m.(ha(m, e1, e2))) else False fi ))

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